

house p

$$\begin{aligned}(C_t^p)^{-\sigma} &= \lambda_t^p \\ \psi(L_t^p)^\varphi &= \lambda_t^p (1 - \tau_m^G) W_t^p \\ \lambda_t^p &= \beta_p E_t \left(\frac{\lambda_{t+1}^p r_t^b}{\pi_{t+1}} \right) \\ q_t^p &= \beta_p E_t \left\{ \frac{\lambda_{t+1}^p}{\lambda_t^p} [r_{t+1}^k + (1 - \delta_k) q_{t+1}^p] \right\} \\ 1 &= q_t^p \left[1 - \frac{\Omega}{2} \left(\frac{i_t^p}{i_{t-1}^p} - 1 \right)^2 - \Omega \left(\frac{i_t^p}{i_{t-1}^p} \right) \left(\frac{i_t^p}{i_{t-1}^p} - 1 \right) \right] + \Omega \beta_p E_t \left\{ q_{t+1}^p \frac{\lambda_{t+1}^p}{\lambda_t^p} \left[\left(\frac{i_{t+1}^p}{i_t^p} \right)^2 \left(\frac{i_{t+1}^p}{i_t^p} - 1 \right) \right] \right\} \\ K_t^p &= (1 - \delta_k) K_{t-1}^p + \left[1 - \frac{\Omega}{2} \left(\frac{i_t^p}{i_{t-1}^p} - 1 \right)^2 \right] i_t^p \\ C_t^p + i_t^p + d_t^p &= r_t^k K_{t-1}^p + \frac{r_{t-1}^b}{\pi_t} d_{t-1}^p + (1 - \tau_m^G) W_t^p L_t^p + T_{G,t}\end{aligned}$$

house e

$$\begin{aligned}(C_t^e)^{-\sigma} &= \lambda_t^e \\ \psi(L_t^e)^\varphi &= \lambda_t^e (1 - \tau_m^G) W_t^e \\ \lambda_t^e &= \beta_e E_t \left(\frac{\lambda_{t+1}^e r_t^b}{\pi_{t+1}} \right) \\ q_t^e &= \beta_e E_t \left\{ \frac{\lambda_{t+1}^e}{\lambda_t^e} [r_{t+1}^k + (1 - \delta_k) q_{t+1}^e] \right\} \\ 1 &= q_t^e \left[1 - \frac{\Omega}{2} \left(\frac{i_t^e}{i_{t-1}^e} - 1 \right)^2 - \Omega \left(\frac{i_t^e}{i_{t-1}^e} \right) \left(\frac{i_t^e}{i_{t-1}^e} - 1 \right) \right] + \Omega \beta_e E_t \left\{ q_{t+1}^e \frac{\lambda_{t+1}^e}{\lambda_t^e} \left[\left(\frac{i_{t+1}^e}{i_t^e} \right)^2 \left(\frac{i_{t+1}^e}{i_t^e} - 1 \right) \right] \right\} \\ K_t^e &= (1 - \delta_k) K_{t-1}^e + \left[1 - \frac{\Omega}{2} \left(\frac{i_t^e}{i_{t-1}^e} - 1 \right)^2 \right] i_t^e \\ C_t^e + i_t^e + d_t^e &= r_t^k K_{t-1}^e + \frac{r_{t-1}^b}{\pi_t} d_{t-1}^e + (1 - \tau_m^G) W_t^e L_t^e\end{aligned}$$

government

$$g_t + \frac{r_{t-1}^b}{\pi_t} d_t + \tau_{D,t}^R S_t + T_{G,t} = d_t + \tau_m^G (W_t^p L_t^p + W_t^e L_t^e)$$

central bank

$$\frac{r_t^b}{r^b} = \left(\frac{r_{t-1}^b}{r^b} \right)^{\rho_r} \left[\left(\frac{\pi_t}{\pi} \right)^{\Phi_\pi} \left(\frac{Y_t}{Y} \right)^{\Phi_Y} \right]^{1-\rho_r} e^{\varepsilon_t^m}$$

medi um goods

$$\begin{aligned}r_t^k &= \beta_0(1-\gamma)mc_t \frac{Y_t}{K_{t-1}} \\W_t^p &= (1-\beta_0)(1-\gamma)mc_t \frac{Y_t}{L_{pf,t}} \\W_t^e &= (1-\beta_1)\gamma mc_t \frac{Y_t}{L_{ef,t}} \\\pi_t(\pi_t - \pi) &= \beta_p E_t \left[\frac{\lambda_{t+1}^p}{\lambda_t^p} \pi_{t+1} (\pi_{t+1} - \pi) \frac{Y_{t+1}}{Y_t} \right] + \frac{\varepsilon}{\theta} \left(mc_t - \frac{\varepsilon - 1}{\varepsilon} \right) \\Y_t &= C_t + i_t + g_t + (1 + \tau_{D,t}^R) S_t + \frac{\theta}{2} (\pi_t - \pi)^2 Y_t \\Y_t &= [(K_t)^{\beta_0} (L_{pf,t})^{1-\beta_0}]^{1-\gamma} [(D_t)^{\beta_1} (L_{pf,t})^{1-\beta_1}]^\gamma \\C_t &= C_t^p + C_t^e \\K_t &= K_t^p + K_t^e \\i_t &= i_t^p + i_t^e \\dt &= d_t^p + d_t^e \\L_t &= L_t^p + L_t^e \\L_t^p &= L_{pf,t} \\L_t^e &= L_{pf,t} + L_{D,t}^e\end{aligned}$$

research

$$\begin{aligned}D_{V,t} &= \chi_t^Y Y_t \\D_{G,t} &= \chi_t^C C_t \\N_t^D &= \omega_D [(1 + \tau_{D,t}^R) S_t]^\alpha (L_{D,t}^e)^{1-\alpha} + (1 - \delta_D) N_{t-1}^D \\B_t &= D_{G,t}^\nu (N_t^D)^{1-\nu} \\D_t &= \xi D_{V,t} + (1 - \xi) B_t \\S_t + W_t^e L_{D,t}^e &= Y_t \left[1 - (1 - \beta_1 \gamma) mc_t - \frac{\theta}{2} (\pi_t - \pi)^2 \right] \\W_t^e &= \omega_D (1 - \alpha)^2 \frac{Y_t \left[1 - (1 - \beta_1 \gamma) mc_t - \frac{\theta}{2} (\pi_t - \pi)^2 \right]}{D_t} \left(\frac{D_{G,t}}{N_t^D} \right)^\nu \left[\frac{(1 + \tau_{D,t}^R) S_t}{L_{D,t}^e} \right]^\alpha\end{aligned}$$

shocks

$$\log(T_{G,t}) = (1 - \rho_{TG})\log(\overline{T_G}) + \rho_{TG}\log(T_{G,t-1}) + \varepsilon_t^{T_G}$$
$$\varepsilon_t^{T_G} \sim N(0, \sigma_{T_G}^2)$$

$$\log(\chi_t^Y) = (1 - \rho_{\chi^Y})\log(\overline{\chi^Y}) + \rho_{\chi^Y}\log(\chi_{t-1}^Y) + \varepsilon_t^{\chi^Y}$$
$$\varepsilon_t^{\chi^Y} \sim N(0, \sigma_{\chi^Y}^2)$$

$$\log(\chi_t^C) = (1 - \rho_{\chi^C})\log(\overline{\chi^C}) + \rho_{\chi^C}\log(\chi_{t-1}^C) + \varepsilon_t^{\chi^C}$$
$$\varepsilon_t^{\chi^C} \sim N(0, \sigma_{\chi^C}^2)$$

$$\log(g_t) = (1 - \rho_g)\log(\overline{g}) + \rho_g\log(g_{t-1}) + \varepsilon_t^g$$
$$\varepsilon_t^g \sim N(0, \sigma_g^2)$$

$$\varepsilon_t^m \sim N(0, \sigma_m^2)$$