

Appendix

7.1 A Benchmark Model: Social Planer's Problem

In this section, we provide optimality conditions for social planer's problem of benchmark model with perfect information. We discuss SSP with two different scenarios: with a perfect competitive capital market (in a new classical fashion) and without a capital market.

7.1.1 Without a Capital Market

The social planer makes consumption, investment and labor decisions for each location i in each period t . In period $t + 1$, the firm in location i can not borrow any capital other than social planer's investment in last period. At the same time, labor demand also meets natural constraint \bar{L}_i .

$$\max_{\{C_t, Y_{ft}, K_{it}, L_{it}, X_{j \rightarrow i, t}, Y_{i \rightarrow f, t}, Y_{it}, M_{it}\}} \mathbb{E}_0 \sum_{t=0}^{\infty} \beta^t (\log C_t)$$

Subject to the following conditions:

$$C_t + \sum_{i=1}^N [K_{it+1} - (1 - \delta_i)K_{it}] \leq Y_{ft} \quad (16)$$

$$Y_{ft} = \left(\sum_{i=1}^n a_i^{\frac{1}{\sigma}} Y_{i \rightarrow f, t}^{\frac{\sigma-1}{\sigma}} \right)^{\frac{\sigma}{\sigma-1}} \quad (17)$$

$$Y_{i \rightarrow f, t} + \sum_{j=1}^N X_{i \rightarrow j, t} = Y_{it} \quad (18)$$

$$Y_{it} = A_{it} ((K_{it})^{\alpha_i} L_{it}^{1-\alpha_i})^{\theta_i} M_{it}^{1-\theta_i} \quad (19)$$

$$M_{it} = \prod_{j=1}^N X_{j \rightarrow i, t}^{\gamma_{ji}}, \text{ where } \sum_{j=1}^N \gamma_{ji} = 1 \quad (20)$$

$$L_{it} \leq \bar{L}_i \quad (21)$$

At stage $t = 0$, K_{i0} is given as endowment at each location. The household uses all endowment to produce Y_{f0} , and balance C_0 and K_{i1}^s for all i . Then this process continues to infinity. Notice that we can reduce state space dimension by combining (16), (17) and combining (18), (19) and (20):

$$\max_{\{C_t, K_{it}, L_{it}, X_{j \rightarrow i, t}\}} \mathbb{E}_0 \sum_{t=0}^{\infty} \beta^t (\log C_t)$$

Subject to the following conditions:

$$C_t + \sum_{i=1}^N [K_{it+1} - (1 - \delta_i)K_{it}] \leq \left(\sum_{i=1}^n a_i^{\frac{1}{\sigma}} Y_{i \rightarrow f,t}^{\frac{\sigma-1}{\sigma}} \right)^{\frac{\sigma}{\sigma-1}} \quad (22)$$

$$Y_{i \rightarrow f,t} + \sum_{j=1}^N X_{i \rightarrow j,t} = A_{it} (K_{it}^{\alpha_i} L_{it}^{1-\alpha_i})^{\theta_i} (\prod_{j=1}^N X_{j \rightarrow i,t}^{\gamma_{ji}})^{1-\theta_i}, \text{ where } \sum_{j=1}^N \gamma_{ji} = 1 \quad (23)$$

$$L_{it} \leq \bar{L}_i \quad (24)$$

$$\begin{aligned} \mathcal{L} = & \sum_{t=0}^{\infty} \beta^t \left\{ \log C_t + \mu_t \cdot \left[\left(\sum_{i=1}^n a_i^{\frac{1}{\sigma}} Y_{i \rightarrow f,t}^{\frac{\sigma-1}{\sigma}} \right)^{\frac{\sigma}{\sigma-1}} - C_t - \sum_{i=1}^N (K_{it+1} - (1 - \delta_i)K_{it}) \right] \right. \\ & + \sum_{i=1}^N \lambda_{it} \cdot \left[A_{it} (K_{it}^{\alpha_i} L_{it}^{1-\alpha_i})^{\theta_i} (\prod_{j=1}^N X_{j \rightarrow i,t}^{\gamma_{ji}})^{1-\theta_i} - Y_{i \rightarrow f,t} - \sum_{j=1}^N X_{i \rightarrow j,t} \right] \\ & \left. + \sum_{i=1}^N \xi_{it} \cdot [\bar{L}_i - L_{it}] \right\} \end{aligned}$$

First order conditions are given by:

$$[C_t]: \quad \frac{1}{C_t} = \mu_t \quad (25)$$

$$[K_{it}]: \quad \beta[\mu_t(1 - \delta_i) + \lambda_{it}\alpha_i\theta_i \frac{Y_{it}}{K_{it}}] = \mu_{t-1} \quad (26)$$

$$[L_{it}]: \quad \lambda_{it}(1 - \alpha_i)\theta_i \frac{Y_{it}}{L_{it}} = \xi_{it} \quad (27)$$

$$[Y_{i \rightarrow f,t}]: \quad \lambda_{it} = \mu_t \left(\sum_{i=1}^n a_i^{\frac{1}{\sigma}} Y_{i \rightarrow f,t}^{\frac{\sigma-1}{\sigma}} \right)^{\frac{1}{\sigma-1}} a_i^{\frac{1}{\sigma}} Y_{i \rightarrow f,t}^{-\frac{1}{\sigma}} \quad (28)$$

$$[X_{j \rightarrow it}]: \quad \lambda_{it} \cdot (1 - \theta_i)\gamma_{ji} \frac{Y_{it}}{X_{j \rightarrow it}} - \lambda_{jt} = 0 \quad (29)$$

Once C_t and K_{it+1} are pinned down, Y_{ft} is also determined. M_{it} is pinned down by $X_{j \rightarrow it}$. So as Y_{it} and $Y_{i \rightarrow ft}$.

7.1.2 With a Capital Market

One might concern that dysfunction capital market might be too strict, so in this section we discuss social planner's problem with a functioning capital market. In this scenario, the social planner decides consumption C_t , capital distribution K_{it} and total investment decision