C Summary of the theoretical model

The model in is fully described by the following sets of variables:

- Prices: π_t , W_t/P_t , $r_{t,t+1}$
- Interest rates: R_t
- Allocations: C_t, Y_t, H_t, λ_t
- Shocks: $\sigma_{r,t}, \epsilon_{r,t}, \epsilon_{\sigma,t}$

Equations describing the model are given by:

$$\lambda_t = 1/(C_t - \alpha C_{t-1})$$
$$\lambda_t = \beta E_t \lambda_{t+1} \left(\frac{R_t}{\pi_{t+1}}\right) r_{t,t+1} = 1/R_t$$
$$\lambda_t \frac{W_t}{P_t} = H_t^{\eta - 1}$$
$$Y_t = H_t$$

$$\begin{aligned} \theta - 1 &= \theta \frac{W_t}{P_t} - \phi \left(\frac{\pi_t}{\pi} - 1\right) \left(\frac{\pi_t}{\pi}\right) + \beta \phi E_t \left[\frac{\lambda_{t+1}}{\lambda_t} \left(\frac{\pi_{t+1}}{\pi} - 1\right) \left(\frac{\pi_{t+1}}{\pi}\right) \left(\frac{Y_{t+1}}{Y_t}\right)\right] \\ Y_t &= C_t + \frac{\phi}{2} Y_t \left(\frac{\pi_t}{\pi} - 1\right)^2 \\ \frac{R_t}{R} &= \left(\frac{R_{t-1}}{R}\right)^{\rho_r} \left(\frac{\pi_t}{\pi}\right)^{\rho_\pi} \left(\frac{Y_t}{Y_{t-1}}\right)^{\rho_y} e^{\sigma_{r,t}} e^{\epsilon_{r,t}} \\ \sigma_{r,t} &= \rho_\sigma \sigma_{r,t-1} + q_\sigma \epsilon_{\sigma,t} \\ \epsilon_{r,t} \sim N(0,1) \\ \epsilon_{\sigma,t} \sim N(0,1) \end{aligned}$$

The deterministic steady state, given parameters set in calibration, is described by:

$$\begin{aligned} \pi &= 1.005 \\ R &= \pi/\beta \\ r &= 1/R \\ \frac{W}{P} &= \frac{\theta-1}{\theta(1-\alpha)} \\ H &= \left(\frac{\theta-1}{\theta(1-\alpha)}\right)^{1/\eta} \\ Y &= \left(\frac{\theta-1}{\theta(1-\alpha)}\right)^{1/\eta} \\ C &= \left(\frac{\theta-1}{\theta(1-\alpha)}\right)^{1/\eta} \\ \lambda &= \left(\frac{\theta(1-\alpha)}{\theta-1}\right)^{1/\eta} \end{aligned}$$