

$$\hat{r}_\tau^* = \frac{(1 - \beta)}{\beta} E_\tau \sum_{i=\tau+1}^{\infty} \beta^{i-\tau} \hat{r}_{i-1},$$