

$$(1-\theta)\frac{\Lambda_t}{P_t} \exp\left\{\left[\frac{\lambda\sigma_\varepsilon^2+(1-\lambda)\sigma_z^2}{\lambda^2\sigma_\varepsilon^2+(1-\lambda)^2\sigma_z^2+\sigma_v^2}(\lambda\log \varepsilon_t+(1-\lambda)\log Z_t+v_t)\right]+\frac{1}{2}\Omega_s\right\}-\Lambda_t\Phi_p\left(\frac{P_t}{P_{t-1}}-1\right)\frac{Y_t}{P_{t-1}}+\xi_t-\beta\Phi_p\left[-\frac{P_{t+1}}{P_t^2}\left(\frac{P_{t+1}}{P_t}-1\right)\Lambda_{t+1}Y_{t+1}\right]=0$$

Since ε_{jt} and z_t are Gaussian, the conditional variance Ω_s will not depend on the observed s_{jt} and will be given by

$$\Omega_s = \text{var}\left[(\varepsilon_{jt} + z_t) | s_{jt}\right] = \text{var}(\varepsilon_{jt} + z_t) - \frac{[\text{cov}(\varepsilon_{jt} + z_t, s_{jt})]^2}{\text{var}(s_{jt})}$$

$$\text{var}(s_{jt}) = \lambda^2\sigma_\varepsilon^2 + (1-\lambda)^2\sigma_z^2 + \sigma_v^2$$

$$\text{cov}(\varepsilon_{jt} + z_t, s_{jt}) = \lambda\sigma_\varepsilon^2 + (1-\lambda)\sigma_z^2$$

$$s_{jt} = \lambda\log \varepsilon_{jt} + (1-\lambda)\log Z_t + v_{jt} = \lambda\varepsilon_{jt} + (1-\lambda)z_t + v_{jt}$$

$$(1-\theta)\frac{\Lambda_t}{P_t} \exp\left\{[A(\lambda\log \varepsilon_t+(1-\lambda)\log Z_t+v_t)]+\frac{1}{2}\Omega_s\right\}-\Lambda_t\Phi_p\left(\frac{P_t}{P_{t-1}}-1\right)\frac{Y_t}{P_{t-1}}+\xi_t-\beta\Phi_p\left[-\frac{P_{t+1}}{P_t^2}\left(\frac{P_{t+1}}{P_t}-1\right)\Lambda_{t+1}Y_{t+1}\right]=0$$

$$A = \frac{\lambda\sigma_\varepsilon^2+(1-\lambda)\sigma_z^2}{\lambda^2\sigma_\varepsilon^2+(1-\lambda)^2\sigma_z^2+\sigma_v^2}$$

$$(1-\theta)\frac{\Lambda_t}{P_t} \varepsilon_t^{A\lambda} Z_t^{A(1-\lambda)} \exp\left\{Av_t + \frac{1}{2}\Omega_s\right\} - \Phi_p \frac{\Lambda_t P_t Y_t}{P_{t-1}^2} + \Phi_p \frac{\Lambda_t Y_t}{P_{t-1}} + \xi_t + \beta\Phi_p \frac{P_{t+1}^2 \Lambda_{t+1} Y_{t+1}}{P_t^3} - \beta\Phi_p \frac{P_{t+1} \Lambda_{t+1} Y_{t+1}}{P_t^2} = 0$$

$$\Phi_p \frac{\Lambda_t P_t Y_t}{P_{t-1}^2} = \Phi_p \frac{\bar{\Lambda} e^{\hat{\Lambda}_t} \bar{P} e^{\hat{P}_t} \bar{Y} e^{\hat{Y}_t}}{\bar{P}^2 e^{2\hat{P}_{t-1}}} = \Phi_p \frac{\bar{\Lambda} \bar{Y}}{\bar{P}} \frac{e^{\hat{\Lambda}_t} e^{\hat{P}_t} e^{\hat{Y}_t}}{e^{2\hat{P}_{t-1}}} = \Phi_p \frac{\bar{\Lambda} \bar{Y}}{\bar{P}} (1 + \hat{\Lambda}_t)(1 + \hat{P}_t)(1 + \hat{Y}_t)(1 - 2\hat{P}_{t-1}) =$$

$$= \Phi_p \frac{\bar{\Lambda} \bar{Y}}{\bar{P}} \left[1 + \hat{\Lambda}_t + \hat{P}_t + \hat{\Lambda}_t \hat{P}_t \right] \left[1 + \hat{Y}_t - 2\hat{P}_{t-1} - \overbrace{2\hat{Y}_t \hat{P}_{t-1}}^{\approx 0} \right] =$$

$$= \Phi_p \frac{\bar{\Lambda} \bar{Y}}{\bar{P}} \left\{ 1 + \hat{Y}_t - 2\hat{P}_{t-1} + \hat{\Lambda}_t + \hat{\Lambda}_t \hat{Y}_t - 2\hat{\Lambda}_t \hat{P}_{t-1} + \hat{P}_t + \hat{P}_t \hat{Y}_t - 2\hat{P}_t \hat{P}_{t-1} \right\}$$

$$= \Phi_p \frac{\bar{\Lambda} \bar{Y}}{\bar{P}} (1 + \hat{\Lambda}_t + \hat{Y}_t + \hat{P}_t - 2\hat{P}_{t-1})$$