

Firms

$$s_{jt} = \lambda \log \epsilon_{jt} + (1 - \lambda) \log Z_t + v_{jt}$$

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$$Y_t \equiv \left[\int_0^1 \epsilon_{jt}^{1/\theta} Y_{jt}^{(\theta-1)/\theta} dj \right]^{\theta/(\theta-1)}$$

$$\max_{Y_{jt}} E \left\{ P_t \left[\int_0^1 \epsilon_{jt}^{1/\theta} Y_{jt}^{(\theta-1)/\theta} dj \right]^{\theta/(\theta-1)} - \int_0^1 P_{jt} Y_{jt} dj \right\}$$

$$Y_{jt} \equiv \left(\frac{P_{jt}}{P_t} \right)^{-\theta} \epsilon_{jt} Y_t$$

$$Y_t(j) = A_t N_t(j) K_t(j)$$

$$\log A_t = (1 - \rho_A) \log(\bar{A}) + \rho_A \log(A_{t-1}) + e_{At}$$

$$\Pi_{jt} = P_{jt} Y_{jt} - W_t N_{jt} - R_t K_{jt}$$

$$\max_{N_{jt}, K_{jt}} E \left[\left(P_t Y_{jt}^{-\frac{1}{\theta}} [\epsilon_{jt} Y_t]^{\frac{1}{\theta}} Y_{jt} - W_t N_{jt} - R_t K_{jt} \right) \middle| S_{jt} \right]$$

$$\left(1 - \frac{1}{\theta} \right) [A_t K_{jt}]^{1-\frac{1}{\theta}} N_{jt}^{-1/\theta} P_t E \left[[\epsilon_{jt} Z_t]^{1/\theta} \middle| s_{jt} \right] - W_t = 0$$

$$\left(1 - \frac{1}{\theta} \right) Y_{jt}^{1-\frac{1}{\theta}} P_t E \left[[\epsilon_{jt} Z_t]^{1/\theta} \middle| s_{jt} \right] = W_t N_{jt}$$

Get Logarithm

$$\log\left(1 - \frac{1}{\theta}\right) + \left(1 - \frac{1}{\theta}\right)y_{jt} + p_t + E\left[\frac{1}{\theta}\varepsilon_{jt} + \frac{1}{\theta}z_t \mid s_{jt}\right] = w_t + n_{jt}$$

$$E\left[\frac{1}{\theta}\varepsilon_{jt} + \frac{1}{\theta}z_t \mid s_{jt}\right] = \frac{\text{cov}\left(\frac{1}{\theta}\varepsilon_{jt} + \frac{1}{\theta}z_t, s_{jt}\right)}{\text{var}(s_{jt})} s_{jt} = \frac{\frac{1}{\theta}\lambda\sigma_\varepsilon^2 + \frac{1}{\theta}(1-\lambda)\sigma_z^2}{\lambda^2\sigma_\varepsilon^2 + (1-\lambda)^2\sigma_z^2 + \sigma_v^2} (\lambda\varepsilon_{jt} + (1-\lambda)z_t + v_{jt})$$

$$\log\left(1 - \frac{1}{\theta}\right) + \left(1 - \frac{1}{\theta}\right)y_{jt} + p_t + \frac{\frac{1}{\theta}\lambda\sigma_\varepsilon^2 + \frac{1}{\theta}(1-\lambda)\sigma_z^2}{\lambda^2\sigma_\varepsilon^2 + (1-\lambda)^2\sigma_z^2 + \sigma_v^2} (\lambda\varepsilon_{jt} + (1-\lambda)z_t + v_{jt}) = w_t + n_{jt}$$