

$$(1-\theta) \frac{\Lambda_t}{P_t} \exp \left\{ \left[\frac{\lambda \sigma_\varepsilon^2 + (1-\lambda) \sigma_z^2}{\lambda^2 \sigma_\varepsilon^2 + (1-\lambda)^2 \sigma_z^2 + \sigma_v^2} (\lambda \log \varepsilon_t + (1-\lambda) \log Z_t + v_t) \right] + \frac{1}{2} \Omega_s \right\} - \Lambda_t \Phi_p \left(\frac{P_t}{P_{t-1}} - 1 \right) \frac{Y_t}{P_{t-1}} + \xi_t - \beta \Phi_p \left[-\frac{P_{t+1}}{P_t^2} \left(\frac{P_{t+1}}{P_t} - 1 \right) \Lambda_{t+1} Y_{t+1} \right] = 0$$

Since ε_{jt} and z_t are Gaussian, the conditional variance Ω_s will not depend on the observed s_{jt} and will be given by

$$\Omega_s = \text{var} \left[(\varepsilon_{jt} + z_t) \middle| s_{jt} \right] = \text{var}(\varepsilon_{jt} + z_t) - \frac{\left[\text{cov}(\varepsilon_{jt} + z_t, s_{jt}) \right]^2}{\text{var}(s_{jt})}$$

$$\text{var}(s_{jt}) = \lambda^2 \sigma_\varepsilon^2 + (1-\lambda)^2 \sigma_z^2 + \sigma_v^2$$

$$\text{cov}(\varepsilon_{jt} + z_t, s_{jt}) = \lambda \sigma_\varepsilon^2 + (1-\lambda) \sigma_z^2$$

$$s_{jt} = \lambda \log \varepsilon_{jt} + (1-\lambda) \log Z_t + v_{jt} = \lambda \varepsilon_{jt} + (1-\lambda) z_t + v_{jt}$$